Article

Theoretical Insights into the Resonant Suppression Effect in Vibrational Polariton Chemistry

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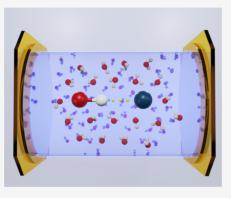
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ABSTRACT: Recent experiments demonstrated the possibilities of modifying groundstate chemical reaction rates by placing an ensemble of molecules in an optical microcavity through a resonant coupling between the cavity mode and molecular vibrations. Typical VSC experiments operate in the absence of any light source. The VSC-induced rate constant suppression occurs under the resonance condition when the cavity frequency matches the molecular vibrational frequency, and only under the normal incidence when considering in-plane momentum inside a Fabry—Pérot cavity. In this work, we use quantum dynamics simulations and analytic theories to provide valuable insights into observed VSC phenomena, including the resonance behavior, the nonlinear change of the rate constant when increasing Rabi splitting, modification of both reactive enthalpy and entropy, and a reason why, with a very low barrier, there is a lack of the cavity modification. The analytic theory also exhibits the normal incidence condition and collective coupling effects.



INTRODUCTION

Recent experiments^{1–10} by Ebbesen, Simpkins, and others demonstrated that chemical reaction rate constants could be suppressed^{1,7} or enhanced^{8–11} by resonantly coupling molecular vibrations to quantized radiation modes inside a Fabry–Pérot (FP) microcavity.^{12–14} This effect, known as vibrational strong coupling (VSC) modified ground-state chemical reactivity, has the potential to selectively slow down competing reactions² or speed up a target reaction, thus achieving mode selectivity^{2,15} and offering new chemical transformation strategies in synthetic chemistry.

There are several characteristic, universal phenomena in the VSC experiments,^{12,13,16,17} including (1) the resonance effect,^{1,7} where the maximum VSC effect occurs when the cavity frequency is tuned to the vibrational frequency $\omega_{\rm c} = \omega_{\rm O}$; (2) the normal incidence effect, 1 where the VSC effect only happens when the in-plane photon momentum is $k_{\parallel} = 0$; (3) the collective effect^{1,4,8} where the magnitude of VSC modification increases when increasing the number of molecules N; (4) the reaction is under thermal activation without any optical pumping.^{1,2} To the best of our knowledge, there is no unified, microscopic theory that can explain all of the above-observed phenomena, $^{16-19}$ despite many insightful hypothesis and mechanisms^{7,15,20-42} that have been proposed to explain the VSC effects. In particular, there is no analytic rate constant theory that could explain the sharp resonance suppression behavior. The transition state theory (TST) predicts no frequency-dependent VSC effects,^{20,25} and existing rate constant theory often depends on the barrier frequency, or has a very broad cavity-frequency dependence for the rate changes.^{20,21,32,43} These difficulties in using the existing rate theories to explain the sharp resonance VSC effects hint that a proper mechanistic description of the VSC resonance suppression might need a completely new analytic rate constant expression. Recently, several key theoretical advances^{21,44} have demonstrated that a sharp resonance enhancement of the rate constant occurs when using a quantum state description of the vibrational states, a finding verified by exact quantum dynamics simulations.^{21,44–46}

In this work, we present a microscopic theory and mechanism that provide insights into understanding the characteristic features of the observed VSC effects mentioned above. We consider a theoretical model where a cavity mode couples to a set of solvent vibrations $\{Q_j\}$ (spectator modes, or rate-promoting vibrations) which in turn couple to a reaction coordinate R_0 . This model captures the key features of recent VSC experiments^{1,7} and has been employed in previous theoretical studies on VSC-modified reactivities.^{21,31} It also reflects the characteristics observed in theoretical simulations of polaritonic vibrational energy relaxation,²⁹ which demonstrate collective and resonance behavior. We derive an analytic rate constant expression based on Fermi's Golden Rule (FGR) and employ numerically exact quantum dynamics simulations to demonstrate the accuracy of the theory. The theory provides

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theoretical insights into the resonance VSC suppression of the rate constant under normal-incidence conditions, collective light-matter coupling, and the thermally activated regime.

METHODS

Theoretical Model. We use the Pauli–Fierz (PF) Hamiltonian to describe the light-matter interaction of molecular vibrations in an optical cavity, ^{17,47} expressed as follows

$$\hat{H} = \hat{H}_0 + \hat{H}_Q + \hat{H}_{\rm LM} + \hat{H}_{\nu} + \hat{H}_{\rm loss}$$
(1)

where $\hat{H}_0 = \hat{T}_0 + \hat{V}(\hat{R}_0)$ is the Hamiltonian of the reactive mode, with the reaction coordinate \hat{R}_0 , and ground state potential energy surface as a symmetric double well potential along R_0 . We use a set of localized diabatic vibrational states, $|\nu_L\rangle$ and $|\nu_R\rangle$ to represent ground vibrational states associated with the left well (reactant) and the right well (product), as well as $|\nu_L'\rangle$ and $|\nu_R'\rangle$ associated with the vibrational excited states, depicted in Figure 1d. In this picture, the vibrational

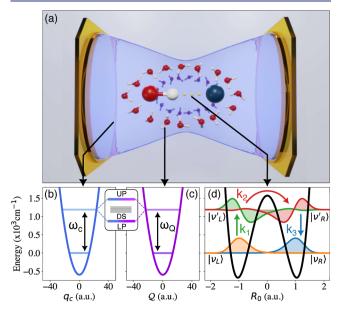


Figure 1. Schematic illustration of the VSC-modified reactions and the mechanisms. (a) Schematic illustration of a reactive molecule whose reaction coordinate is coupled to a set of solvent vibrations, which are in turn coupled to a cavity mode. (b) Photonic potential coupled to (c) an intermolecular vibration whose hybridization leads to a set of polaritonic states with Rabi splitting Ω_R . The intermolecular vibration, in turn, couples to a reaction coordinate R_0 . (d) Potential energy surface of the chemical reaction along the reaction coordinate, with four key vibrational states visualized.

frequency ω_0 for the reactant is defined as the transition frequency associated with $|\nu_L\rangle \rightarrow |\nu'_L\rangle$, that is $\omega_0 \equiv (E_{\nu'_L} - E_{\nu L})/\hbar$. The details of the vibrational states and the description of \hat{H}_{ν} and \hat{H}_{loss} are provided in Supporting Information, Section 1.

We further consider that the reaction coordinate \hat{R}_0 is coupled to a set of nonreactive spectator modes $\{Q_j\}$. We model the interactions between Q modes and R_0 using the Hamiltonian²¹

$$\hat{H}_{Q} = \sum_{j=1}^{N} \frac{\hat{\Pi}_{j}^{2}}{2} + \frac{\omega_{\rm Q}^{2}}{2} \left(\hat{Q}_{j} - \frac{C_{j}}{\omega_{\rm Q}^{2}} \hat{R}_{0} \right)^{2}$$
(2)

where $\hat{\Pi}_j$ and \hat{Q}_j are the momentum and coordinate for the Q modes, with coupling strength C_j . These modes have a uniform frequency ω_{Q} . This model captures essential features of several VSC reactions. For example, in ref 1, the C–Si is the R_0 reaction coordinate, and Si– $(Me)_3$ is nonreactive Q mode that strongly couple to R_0 (for N = 1). In ref 7, the spectator mode Q could be the N–C–O vibrational mode in the reactant (for N = 1). The solvent vibrations could also be viewed as the spectator mode $\{Q_j\}$ (for $N \gg 1$), which was studied in the recent VSC theoretical investigations.^{21,31}

We define the reorganization energy for R_0 caused by Q_j coupling as

$$\Lambda = \sum_{j=1}^{N} C_j^2 / (2\omega_{\rm Q}^2) \tag{3}$$

Note that Λ is a collective quantity between the reaction coordinate R_0 and the solvent DOF Q_j . For the solvent–solute interactions in eq 2, with an increasing number of solvent molecules, the outer sphere solvents will only be weakly coupled to the solute, while the solvent inner sphere will be strongly coupled, resulting in a solute–solvent distance-specific coupling strength C_j . In this study, we keep Λ as a fixed parameter.

The light-matter interaction Hamiltonian \hat{H}_{LM} considers one cavity mode coupled to the $\{Q_i\}$ modes, expressed as

$$\hat{H}_{\rm LM} = \frac{\hat{p}_{\rm c}^2}{2} + \frac{\omega_{\rm c}^2}{2} \left(\hat{q}_{\rm c} + \sqrt{\frac{2}{\omega_{\rm c}}} \eta_{\rm c} \sum_{j=1}^N \hat{Q}_j \cdot \cos \varphi_j \right)^2 \tag{4}$$

where the photonic position operator $\hat{q}_c = \sqrt{\hbar/(2\omega_c)} (\hat{a}^{\dagger} + \hat{a})$ and momentum operator $\hat{p}_c = i\sqrt{\hbar\omega_c/2} (\hat{a}^{\dagger} - \hat{a})$ are expressed in terms of the photonic creation operator \hat{a}^{\dagger} and annihilation \hat{a} for a given cavity mode, with ω_c as the cavity frequency. A generalization of this term with many cavity modes will be discussed at the end of the paper. Further, $\eta_c = \sqrt{1/(2\hbar\omega_c\epsilon_0 V)}$ is the light-matter coupling strength, where ϵ_0 is the permittivity inside the cavity, and V is the effective quantization volume of that mode. For simplicity, we have assumed that the dipole operators are linear^{21,27} such that $\hat{\mu}(Q_j) \cdot \hat{e}_{\perp} \approx \hat{Q}_j \cdot \cos \varphi_j$, where \hat{e}_{\perp} is the transverse field polarization direction (one of the two inplane directions in a FP cavity^{17,46}). In contrast to the $R_0 - Q_j$ interaction characterized by C_j (electrostatic interactions) which depends on the solute–solvent distance, the cavity mode, on the other hand, interacts with all solvent modes { Q_j } with η_c weighted by $\cos \varphi_j$, resulting in delocalized interactions that can be observed from the Rabi splitting from spectroscopy.⁴⁸

Under the resonance condition of $\omega_c = \omega_{Q_j}$ the total Rabi splitting from the spectral measurements is related to the light-matter coupling strength. When there is no dipole angle disorder (cos $\varphi_j = 1$ for all *j*), the Rabi splitting is expressed as^{16,17,48,49}

$$\Omega_{\rm R} = 2\sqrt{N}\eta_{\rm c}\omega_{\rm c}\mu_{\rm O} \tag{5}$$

the transition dipole matrix element associated with Q_j is expressed as $\mu_Q = \langle 0|\hat{Q}_j|1\rangle$ (for linear dipole approximation²⁰) which is assumed to be identical for all Q_j modes.

Based on this model and the effective spectral density theory, we show how the cavity mode collectively coupled to the spectator modes influences the forward reaction along a reaction coordinate R_0 . We then derive an analytical rate constant using Fermi's Golden Rule (FGR), the accuracy of which is confirmed by numerically exact quantum dynamics simulations via the Hierarchical equations of motion (HEOM) approach.

RESULTS AND DISCUSSIONS

Mechanism and Analytic Rate Constant Expression. Under the thermally activated initial condition, the reaction coordinate R_0 undergoes a barrier-crossing process, where the transition state is reached and finally relaxes to the product

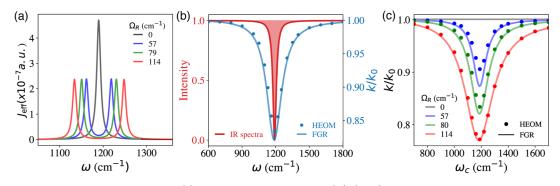


Figure 2. Resonance behavior of the VSC effect. (a) Effective spectral density $J_{eff}(\omega)$ (eq 8) with different values of Ω_{R} , where the two peaks correspond to the polariton modes. (b) VSC enabled rate constant reduction (blue) and the IR spectra (red) for the spectator mode Q_j outside the cavity, both of which occur at $\omega_c = \omega_Q$. The ratio of inside and outside the cavity rate constant k/k_0 obtained from analytic FGR theory (blue solid line) and HEOM (blue solid circles) for N = 1 with $\Omega_R = 57$ cm⁻¹. (c) Normalized rate constant profile k/k_0 (with respect to the outside cavity case k_0) as a function of cavity frequency ω_c and various Ω_R . All calculations are done with a cavity lifetime $\tau_c = 500$ fs. The FGR results (solid lines) are rescaled by a factor of $\alpha = 0.7$ (see eq 7).

configuration. Quantum mechanically, the same process is described as (1) the thermally activated vibrational excitation on the reactant side $|\nu_L\rangle \rightarrow |\nu'_L\rangle$, (2) vibrational excited states transition $|\nu'_L\rangle \rightarrow |\nu'_R\rangle$, and (3) vibrational relaxation on the product side $|\nu'_R\rangle \rightarrow |\nu_R\rangle$. The population dynamics from the HEOM exact simulations (see Supporting Information 4) indicate that the reaction mechanism can be described as follows⁴⁵

$$|\nu_{\rm L}\rangle \stackrel{\kappa_1}{\to} |\nu_{\rm L}'\rangle \stackrel{\kappa_2}{\to} |\nu_{\rm R}'\rangle \stackrel{\kappa_3}{\to} |\nu_{\rm R}\rangle \tag{6}$$

where the initial vibrational excitation $(|\nu_L\rangle \rightarrow |\nu'_L\rangle)$ is the ratelimiting step, such that $k_1 \ll k_2$, k_3 , see Figure 1d. This leads to a steady state population (time-independent plateau population) of the intermediate states $|\nu'_L\rangle$ and $|\nu'_R\rangle$, and the overall rate constant for the entire reaction (k) can be approximate as $k \approx k_1$. The $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition is influenced by the energy exchange between the phonon bath and the spectator modes $\{Q_i\}$. When these spectator modes are resonantly coupled to the cavity, the light-matter hybrid system has a set of polaritonic modes with frequencies $\omega_{\pm} = \omega_{\rm Q} \pm \Omega_{\rm R}/2$, thus effectively removing the influence of Q from the $|\nu_{\rm L}\rangle \rightarrow |\nu'_{\rm L}\rangle$ transition. Another way to understand such influence is the strong coupling between $\{Q_i\}$ and \hat{q}_c causes a fast exchange of energy among them (with frequency Ω_R), and thus effectively decoupled from the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition. This will explicitly decrease the value of k_1 and, as $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ is still the ratelimiting step for the system compiled inside the cavity (see Supporting Information 4), the influence of cavity on k_1 explicitly shows up in the entire apparent rate constant of the reaction because $k \approx k_1$.

Based on this observation, the impact of VSC on the rate is solely attributed to the cavity interacting with the spectator modes, and influencing the rate of the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition, hence imprint its impact on the apparent rate constant of the reaction. This is confirmed by the exact quantum dynamics simulations presented in Figure S2 (Supporting Information 4), where the steady-state population of the $|\nu'_L\rangle$ is suppressed when coupling to the cavity. To develop an analytic theory, we expressed the overall rate constant as $k \approx k_1 = k_D + \alpha \cdot k_{\text{VSC}}$, where k_D is the rate constant for the double-well potential without coupling to any spectator modes Q_j or the cavity mode q_{c} and k_{VSC} the rate provided by the spectator modes with α as a scaling parameter. When FGR is exact and the role of $\{Q_j\}$ and q_c are directly additive to k, $\alpha = 1$. Throughout the paper, we report the ratio of the rate constant inside and outside the cavity as follows

$$k/k_0 = k_{\rm D}/k_0 + \alpha \cdot k_{\rm VSC}/k_0 \tag{7}$$

where k_0 and k_D are directly obtained from HEOM simulations as they are not related to the coupling of the cavity mode. In this work, under the condition $\eta_c = 0$ (outside the cavity), we find that $\alpha \approx 0.7$ will bring the FGR analytic results to quantitatively agree with the numerically exact simulations. This parameter is then fixed for all cases of η_c when coupling the Q mode to the cavity. Note $k_{\rm VSC}$ is the contribution of the spectator modes to the overall rate, thus when $\eta_c = 0$, $k_{\rm VSC}/k_0$ has the largest contribution as the Q modes are in resonance with the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition, promoting the vibrational excitation along R₀. When gradually increasing the light-matter coupling strength, $k_{\rm VSC}/k_0$ will decrease (see eq 11), and eventually goes to zero, such that the Q modes will no longer promote the rate, and $k \sim k_{\rm D}$. In this sense, one can say the resonance VSC between cavity and $\{Q_i\}$ modes includes a "polaron decoupling" $^{50-52}$ between $\{Q_i\}$ and R_0 , slowing down the reaction along R_0 .

We aim to develop an analytic rate constant theory that describes the role of $\{Q_j\}$ and \hat{q}_c on the rate constant. To this end, we derived an effective spectral density, $J_{\text{eff}}(\omega)$, that describes the coupling of $\hat{H}_Q + \hat{H}_{\text{LM}} + \hat{H}_{\text{loss}}$ to the reaction coordinate R_0 , based on the effective spectral density theory.^{53,54} The derivation is provided in Supplementary Note 5, and the general expression is presented in eq S55. A more insightful, approximate form is

$$J_{\rm eff}(\omega) = \frac{\Lambda \cdot \omega_{\rm Q}^2 \cdot \omega \Gamma_{\rm Q}(\omega)}{[\omega_{\rm Q}^2 - \omega^2 + \tilde{\mathcal{R}}(\omega)]^2 + [\omega \Gamma_{\rm Q}(\omega)]^2}$$
(8)

where Λ (defined in eq 3) characterizes the couplings between N spectator Q modes (e.g., solvent DOF) with R_0 , and ω_Q is the solvent frequency which we assume to be identical for all $\{\hat{Q}_j\}$. In addition, Γ_Q characterizes the excitation decay rate in the $\{Q_i\}$ and cavity modes

$$\Gamma_{\rm Q}(\omega) = \frac{2\lambda_{\rm Q}}{\gamma_{\rm Q}} + \frac{2N\chi^2 \cdot \omega_{\rm c}^3 \eta_{\rm c}^2 \tau_{\rm c}^{-1}}{(\omega_{\rm c}^2 - \omega^2)^2 + \omega^2 \tau_{\rm c}^{-2}}$$

where λ_Q and γ_Q are phonon bath parameters for $\{Q_i\}$ modes (see eq S13 in Supporting Information 1), τ_c is the cavity lifetime, and $\omega_{\rm c}$ is the cavity frequency. Further, χ characterizes the angle of the vibrational dipole operator relative to the cavity mode \hat{q}_{c} , with the following expression

$$\chi = \frac{1}{N} \sum_{j} \cos \varphi_{j} \equiv \langle \cos \varphi \rangle \tag{9}$$

Finally, $\hat{\mathcal{R}}(\omega)$ in eq 8 is expressed as

$$\tilde{\mathcal{R}}(\omega) = \frac{2N\chi^2 \cdot \omega_c \eta_c^2 \omega^2}{(\omega_c^2 - \omega^2)^2 + \omega^2 \tau_c^{-2}} \cdot (\omega^2 - \omega_c^2 + \tau_c^{-2})$$

Note that in this approximate form of $J_{\text{eff}}(\omega)$ in eq 8, there are N-1 dark states that do not appear, thus being decoupled³¹ from the reaction coordinate \hat{R}_0 . This is due to a mean-fieldlike approximation for the C_i when deriving eq 8. In the general expression of the spectral density (eq S55), the dark states can still show up (see Figure S5 and S6 in Supporting Information 5) when having disorders. This will be discussed in the Collective coupling mechanism section.

Figure 2a presents $J_{\text{eff}}(\omega)$ at various Ω_{R} . At $\Omega_{\text{R}} = 0$ (black curve), the peak of $J_{\text{eff}}(\omega)$ is located at the frequency of ω_{O} , and the spectator mode effect is at its maximum due to $\omega_{\rm O}$ = ω_0 . Note that this frequency matching between solvent vibration $\omega_{\rm Q}$ and ω_0 has been observed in experiments⁸⁻¹¹ and was referred to as the cooperative coupling,⁸ although the VSC kinetics effect is rate constant enhancement in those studies.^{8–11} In ref 7, the solvent C-H vibration is strongly coupled to the cavity mode, which could also impact the rate constant and leads to a rate constant suppression effect, although the solvent frequency $\omega_{\rm Q}$ seems to be largely detuned from the frequency of ω_0 , likely due to the anharmonic interaction effects⁵⁵ which are not included by the bilinear interaction term in eq 2. As $\Omega_{\rm R}$ increases, $J_{\rm eff}(\omega)$ split into two peaks (corresponding to the two vibrational polariton frequencies $\omega_{\pm} \approx \omega_{\rm Q} \pm \Omega_{\rm R}/2$), and is moving away from ω_0 , hence reducing the spectator mode effect and the value of k_1 for $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition (cf. eq 6). Note that the $J_{\text{eff}}(\omega)$ expression (eq 8) is only sensitive to the collective coupling strength $\Omega_{\rm R}$, and for N > 1, the behavior of $J_{\rm eff}(\omega)$ is identical to N = 1 as long as $\Omega_{\rm R}$ and Λ are identical. The rest of the dark vibrational modes are decoupled from \hat{R}_0 and will not explicitly show up in $J_{\text{eff}}(\omega)$.

To evaluate the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition rate constant $k_{\rm VSC}$ (eq 7), we use the FGR theory expressed as follows

 $k_{\rm VSC}$

$$= 2 \left| \Delta_{x} \right|^{2} \int_{0}^{\infty} \mathrm{d}\omega \frac{\Lambda \omega_{\mathrm{Q}}^{2} \cdot \omega \Gamma_{\mathrm{Q}}(\omega) \cdot \mathcal{A}_{0}(\omega - \omega_{0}) \cdot e^{-\beta \hbar \omega_{0}}}{\left[\omega_{\mathrm{Q}}^{2} - \omega^{2} + \tilde{\mathcal{R}}(\omega) \right]^{2} + \left[\omega \Gamma_{\mathrm{Q}}(\omega) \right]^{2}}, \tag{10}$$

where ω is the transition frequency, ω_0 is the vibrational frequency for the reactive mode R_0 , \mathcal{A}_0 is the broadening function that accounts for the fluctuations in ω_0 (see details in Supporting Information 1), $\Delta_x = \langle \nu_L | \hat{R}_0 | \nu'_L \rangle$ the vibrational transition dipole for the $|\nu_{\rm L}\rangle$ \rightarrow $|\nu_{\rm L}'\rangle$ transition, β \equiv 1/($k_{\rm B}T)$, and $k_{\rm B}$ is the Boltzmann constant.

The $k_{\rm VSC}$ expression in eq 10 is the first key result of this work. Note that the validity of FGR is under the condition

 $\sqrt{\Delta\omega_{
m O}} \cdot |\Delta_x| \ll k_{
m B}T pprox 200~{
m cm}^{-1}$ under T = 300 K, and the "strong coupling condition" $\left(\Omega_{\rm R} \gg \frac{1}{2}\tau_{\rm c}^{-1} + \lambda_{\rm Q}/\gamma_{\rm O}\right)$ will not break the validity of FGR. In this work, the model system has $\sum_{i}^{N} C_{i} |\Delta_{x}| / \sqrt{2\omega_{Q}} \approx 10 \text{ cm}^{-1}$, which was used in ref 21. Further simplifications of eq 8 under the resonance condition $\omega_{\rm c} = \omega_{\rm Q}$ (see Supporting Information 6) indicate a scaling relation

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$$k_{\rm VSC} \propto \frac{1}{\Omega_{\rm R}^2} \propto \frac{1}{N\eta_{\rm c}^2}$$
 (11)

both the HEOM numerical data (Figure 3a) and the experimental results (e.g., Figure 3D in ref 4) can be fitted

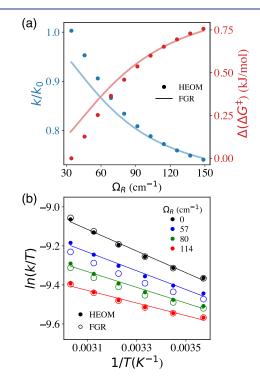


Figure 3. VSC modification of the rate constant predicted by FGR theory (eq 10). (a) Ratio of the rate constant inside and outside the cavity, k/k_0 , and effective free energy barrier change $\Delta(\Delta G^{\ddagger})$ at different $\Omega_{\rm R}$. (b) Eyring plot of $\ln(k/T)$ vs 1/T at various $\Omega_{\rm R}$. In all cases, the cavity is under the resonance condition $\omega_c = \omega_Q$.

well with $k/k_0 = k_D/k_0 + a/(1 + b \cdot \Omega_R^2)$ (with a, b as fitting parameters), details are provided in Supporting Information 6. This scaling relation is the second key result of this work.

VSC Rate Constant Modifications. To validate the $k_{\rm VSC}$ theory in eq 10, we perform numerical simulations of the rate constants for a single spectator mode Q(N = 1) coupled to a single cavity mode, details are provided in Supporting Information 1. For N = 1, the Q mode could be either an intermolecular vibration or a nearby solvent that has a frequency $\omega_{\rm Q} = \omega_0$. Further, we set $\chi = 1$ that corresponds to a vibrational dipole aligned to the cavity mode. All the simulations are performed at T = 300 K and a cavity lifetime τ_c = 500 fs, which are the typical values for the VSC experiments.^{2,7} The exact quantum dynamics propagation is done by using the HEOM approach.⁵⁶⁻⁵⁸ The details of the rate constant calculations are provided in Supporting Information 3.

Figure 2b presents the infrared (IR) profile of the spectator mode (red curve), alongside the cavity-frequency-dependent rate constant profile (blue curve) obtained from the HEOM simulations (blue dots) and the FGR approach (blue solid line, using eq 7). Both profiles exhibit a distinct sharp peak around $\omega_{Q'}$ which is an essential feature observed in most VSC experiments.^{1,7} In particular, existing theories for resonance suppression often have a much broader peak^{20,43} for the rate constant profile (as a function of cavity frequency), which is significantly broader than the width of the line shape, as in those rates theories,^{20,43} the rate constant is not sensitive to ω_Q but rather the partition function expressions (which are influenced by multiple frequencies), resulting in a significantly broader frequency dependence.^{45,59} The new theory in eq 10 is capable of describing a sharp resonance suppression behavior. Reference 21 further demonstrates that for both energy diffusion-limited (see Figure 4 in ref 21) and spatial

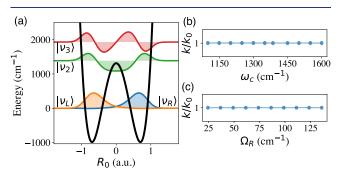


Figure 4. Null results of the VSC effects^{60,61} for a reaction that has a low energy barrier. (a) Reaction Potential along the reaction coordinate R_{0r} with the low reaction barrier^{60,61} such that the vibrational excited states (green and red) are above the barrier, and the mechanistic steps in eq 6 are no longer satisfied. k/k_0 at various (b) cavity frequencies and (c) Ω_{Rr} all showing null VSC reactivities.

diffusion-limited regimes (see Figure S14 in ref 21), resonantly coupled cavity mode to Q will lead to a resonant suppression of the rate constant. The parameters used in our work are under the energy diffusion-limited regime. Meanwhile, ref 21 also demonstrates the resonance enhancement of VSC rate constant when coupling the cavity mode to the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition, which can also be explained by the FGR level of analytic theory in our previous work.⁴⁴

Figure 2c presents the cavity frequency dependence of k/k_0 . Here, the maximum suppression is achieved when $\omega_c = \omega_0$. The VSC suppression effects are enlarged at a larger $\Omega_{R_{I}}$ because the peaks in $J_{\rm eff}(\omega)$ are farther away from the $|\nu_{\rm L}\rangle \rightarrow$ $|\nu'_L\rangle$ transition (as can be seen from Figure 2a). This increase in $\Omega_{\rm R}$ also allows for light-matter interactions at larger cavity detuning, contributing to the broader rate profile. Our analytic FGR expression (eq 10) accurately captures the cavity frequency dependence of the rate constants for a wide range of $\Omega_{\rm R}$. As such, $k_{\rm VSC}$ in eq 10 has achieved a quantitative agreement with the HEOM simulation results and is capable of describing the sharp resonance behavior observed in the experiments.^{1,7} We want to emphasize that the proposed VSC mechanism (eq 6), the shape resonance behavior of k/k_0 as a function of ω_c , as well as the analytic rate constant in eq 10 are robust against the detailed shape of the reactive potential. In Supporting Information 4C, we investigated the model reaction with an asymmetrical double-well potential and verified the validity of the mechanism as well as the sharp

resonance behavior of k/k_{0} , in good agreement with the analytical FGR theory.

Figure 3a presents k/k_0 (blue dots and curve) as a function of $\Omega_{\rm R}$ in the range in which the strong coupling condition is achieved. The results are obtained from HEOM simulations (blue dots), as well as from the FGR analytic expression (blue curve) based on eqs 7 and 10. The results clearly show a nonlinear relation of the rate constant with the Rabi splitting. In particular, at a large Rabi splitting, the maximum suppression of k/k_0 converges to the value of the bare double rate $(k \rightarrow k_{\rm D})$. As shown in Figure 2a, the cavity ultimately removes the effects the spectator mode has on the reaction rate by splitting the spectral density and shifting it away from the frequency of ω_0 . The trend of k/k_0 closely resembles the experimental trend (e.g., Figure 3D in ref 4), and the FGR analytic expression closely agrees with the HEOM results, especially for a large value of Ω_R . The fundamental scaling in eq 11 is also observed in our HEOM results, with details provided in Supporting Information 6. Note that the validity of FGR improves as Ω_{R} increases (FGR results get closer to HEOM). The reason for this "counterintuitive" result is that, in the current theory, Ω_R is not the perturbative parameter. The approximation in eq 10 comes from the perturbative treatment of the $Q - q_c$ DOF coupled to the $|\nu_{\rm L}
angle
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m L}
angle$ transition in the R_0 DOF. As $\Omega_{\rm R}$ increases, the $Q - q_c$ subsystem is further decoupled from the $|\nu_L\rangle \rightarrow |\nu'_L\rangle$ transition, making FGR more accurate.

Figure 3a also presents the change of the effective free energy barrier $\Delta(\Delta G^{\ddagger})$ (red), directly calculated from the rate constant ratio k/k_0 obtained from HEOM simulations (red dots) and FGR (red line). One can interpret the rate constant changes as the change of the effective free energy barrier $\Delta(\Delta G^{\ddagger})$ through^{4,8,45} $\Delta(\Delta G^{\ddagger}) = \Delta G^{\ddagger} - \Delta G_0^{\ddagger} = -k_{\rm B}T \ln(k/k_0)$. Note that this is not an actual change in the free-energy barrier, but rather an effective measure of the purely kinetic effect. Here, one can see a nonlinear relation of $\Delta(\Delta G^{\ddagger})$ with $\Omega_{\rm R}$ that agrees with what has been observed experimentall investigations⁴ suggest a nonlinear trend between $\Delta(\Delta G^{\ddagger})$ and $\Omega_{\rm R}$, and future experimental investigations should focus on measuring more data points to determine the fundamental scaling relations.

Figure 3b presents the temperature dependence of the VSC rate constant using Eyring-type analysis for reactions outside the cavity (black) and inside a resonant cavity under various light-matter coupling strengths (colors). The rate constants were obtained from HEOM simulations (filled circles), and fitted by the least-squares fitting procedure to obtain linearity (thin lines), as well as from FGR rate theory (open circles). If one assumes the rate constant could be described by an Eyringtype equation (transition state theory), then $\ln(k/T) \propto -\frac{\Delta H^{*}}{k_{\rm B}} \cdot \frac{1}{T} + \frac{\Delta S^{*}}{k_{\rm B}}$, where the slope is related to ΔH^{\ddagger} and the y-intercept to ΔS^{\ddagger} . In Figure 3b it can be seen that as $\Omega_{\rm R}$ increases, both ΔH^{\ddagger} and $\Delta \tilde{S}^{\ddagger}$ changes. Here, both the HEOM simulation and the FGR rate theory predict the same trend. We emphasize that based on our current theory, the VSC reaction mechanism is not related to the direct modification of the ΔH^{\ddagger} nor ΔS^{\ddagger} (as also been suggested from the previous theories²⁰), but rather how cavity can mediate vibrational excitations (see eq 6), and described in eq 10.

Another factor that influences the VSC-rate constant is the cavity lifetime τ_c (which also explicitly shows up in the analytic expression of $\Gamma_Q(\omega)$ and $\tilde{\mathcal{R}}(\omega)$. However, we find that k/k_0 is not particularly sensitive to τ_c , and the magnitude of suppression will be maximized under $\tau_c \to \infty$ limit, but start to converge when $\tau_c \geq 300$ fs (see Supporting Information 8).

Null VSC Results due to Low Reaction Barrier. Recent experiments^{60,61} on CN radical-hydrogen atom abstraction reactions do not reveal any noticeable change in the rate constant, even though the molecular system is under the VSC condition. These seemingly null results on the VSC effect could indirectly inform the fundamental mechanism and limitations of VSC-induced rate constant modifications, providing insights into when VSC will not be able to change rate constants (as negative controls). Based on our theory, the cavity can modify the rate constant k_1 , and when $k_1 \ll k_2$, k_3 , such that $k \approx k_1$ (eq 6), the cavity effect on k_1 manifests in the overall rate of reaction k. If the reaction mechanism in eq 6 no longer holds, then coupling to the cavity will not modify the rate constant at all. This will indeed be the case when the potential barrier height is even lower than the first vibrational excited state, and ground state tunneling $|\nu_L\rangle \rightarrow |\nu_R\rangle$ becomes the dominating reactive channel.⁶⁰

To confirm this hypothesis, we contract a model reactive potential depicted in Figure 4a with a lower barrier energy E^{\ddagger} , such that there is only one localized vibrational state, $|\nu_L\rangle$ (orange) in the reactant side. The details of the parameters are provided in Supplemental Note 1 (model 2). The frequency of the spectator mode ω_Q in this model is matched to $|\nu_L\rangle \rightarrow |\nu_2\rangle$ transition. Note that one can still achieve VSC when coupling q_c with Q when $\omega_c = \omega_Q$.

Figure 4b presents the HEOM results of k/k_0 under various cavity frequency ω_c with a strong coupling $\Omega_R = 60 \text{ cm}^{-1}$. We do not observe any noticeable change of k/k_0 over a wide range of cavity frequencies, agreeing with the null experimental results in ref 60. These results can be interpreted from the vibrational population dynamics provided in Figure S3 in Supporting Information 4, where the vibrationally excited states do not actively participate in the forward reaction. Similarly, in ref 61, a range of Ω_R were used in the experiments $(25 \le \Omega_R \le 75 \text{ cm}^{-1})$, and one still finds null VSC results. Figure 4c presents k/k_0 over various Ω_R under the resonance condition $\omega_c = \omega_{Q_1}$ and predicts the same null effect. The current theory based on the mechanism in eq 6 supports the null VSC results recently discovered in the experiments.

As discussed above, we have seen two main mechanisms by which chemical reactions can proceed: (a) the initial vibrational excitation as the limiting reaction step (described by eq 6) and (b) the direct tunneling from reactants to products as the main reactive pathway. Whether a reaction proceeds by the first or second mechanism is dictated by the position of the reaction barrier and the conditions are $E_1^{\ddagger} > \omega_0$ (for case a) or $E_{II}^{\ddagger} < \omega_0$ (for case b), respectively. Thus, for two chemically similar reactions, only the one obeying mechanism (a) will be modified by the VSC effects. Experimental measurements⁶² of the barrier height E^{\ddagger} based on infrared absorption spectroscopy (in conjunction with DFT simulations) suggest that (I) alcoholysis reaction between phenylisocyanate and cyclohexanol has a $E_1^{\ddagger} = 6.7$ kcal/mol (2343 cm⁻¹), and for a similar alcoholysis reaction (II) between 2,4toluene-diisocyanate and chloralhydrate, the activation energy is $E_{II}^{\ddagger} = 2.8 \text{ kcal/mol} (973 \text{ cm}^{-1})$. Interestingly, $E_{I}^{\ddagger} > \{\omega_{0}, \omega_{Q}\} >$

 E_{II}^{\ddagger} and reaction (I) has been investigated by Simpkins et al.⁷ in a cavity under VSC and found a sharp resonance suppression. The current theory thus predicts that coupling reaction (II) to the cavity will give null results (similar to Figure 4) due to its low barrier. Future experiments are encouraged to test this theoretical prediction.

Collective Coupling Effect. The current theory k_{VSC} (eq 10) also exhibits collectiveness of the rate constant modification, originating from the collective coupling between R_0 and $\{Q_i\}$ through \hat{H}_Q in eq 2, and the light-matter couplings between q_c and $\{Q_i\}$ through \hat{H}_{LM} (see eq 4). We consider that N solvent DOF Q_i have identical frequency ω_{Q_i} with details in Supporting Information 5. When C_i are identical, and there is no disorder in the light-matter coupling angles, only the polaritonic states show up in $J_{\text{eff}}(\omega)$ meaning that the N-1dark states present are completely decoupled from the reaction coordinate and will not affect the rate of reaction. This can also be understood from a normal-mode analysis approach³¹ shown in Supporting Information 7. As such, the dark vibrational modes are no longer directly coupled to R₀ and will not influence the rate constant. When there are certain disorders in C_i and also in $\cos \varphi_i$, the dark vibrational modes will have a finite spectral density contribution (see Figures S8 and S9 in Supporting Information 5), and will gradually diminish the VSC collective effect.

Figure 5a presents k/k_0 with $N = 10^4$, at various light-matter coupling strength per molecule $g_c = \eta_c \omega_c \mu_{Q}$ where the

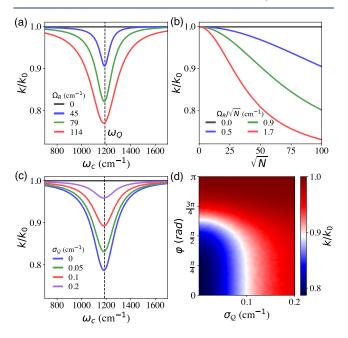


Figure 5. Collective Effect predicted by the FGR theory. (a,b). k/k_0 as a function of (a) the cavity frequency under different $\Omega_{\rm R}$ and (b) Nwhile the light-matter coupling per molecule $g_{\rm c}$ is kept constant, with identical C_j for each vibrational mode. The dipole is assumed to be fully aligned, such that $\chi = 1$. (c) k/k_0 as a function of ω_c , for a system with N = 1000, $\Omega_{\rm R} = 100 \text{ cm}^{-1}$, and $\chi = 1$, with C_j disorder sampled from a normal distribution with σ_Q . (d) k/k_0 for N = 1000, as a function of C_j disorder (σ_Q) and the angle $\{\varphi_j\}$ between the dipole and cavity polarization, which are sampled from a uniform distribution in the range $\{\varphi_i\} \in [0, \pi]$.

collective Rabi splitting is $\Omega_{\rm R} = 2\sqrt{N}g_{\rm c}$ (cf. eq 5). The overall collective coupling between $\{Q_j\}$ and R_0 is kept fixed at $\Lambda = 1.71 \text{ cm}^{-1}$ (see eq 3). Note that as \sqrt{N} always pairs up with $\eta_{\rm c}$ in $k_{\rm VSC}$, the results are thus identical to the case of N = 1 with a much larger $\eta_{\rm c}$. The theory still predicts a sharp resonance suppression when $\omega_{\rm c} = \omega_{\rm O}$.

Figure 5b further present k/k_0 as a function of increasing N, while keeping the light-matter coupling strength per molecule (g_c) a constant, agreeing to the fundamental scaling relation $k_{\rm VSC} \propto 1/N$ in eq 11. The theory demonstrates the same essential feature of the collective coupling effects observed in experiments,⁴ namely the rate constant suppression as the number of molecules (or their concentration) increases. We want to point out that in our early work^{44,45} we have demonstrated the rate constant enhancement based on strong coupling between a single R_0 and q_c . When the cavity mode is explicitly coupled to both Q and R_0 , one would expect competition between these two types of mechanisms.²¹ However, under the collective coupling limit $N \gg 1$, the enhancement effects will be negligibly small as $\eta_c \rightarrow 0$, and the leading effect will be the resonance suppression reported here.

Note that the light-matter coupling strength per molecule, $\eta_c \propto \Omega_{\rm R}/\sqrt{N}$, used in Figure 5 may still be much larger than what is typically expected in VSC experiments. Early theoretical estimates^{16,49} suggest that at least $N = 10^6$ to 10^{12} molecules must be collectively coupled to achieve the experimentally⁴⁸ observed Rabi splitting $\Omega_{\rm R}$. In contrast, recent experimental work by Xiong⁶³ shows as few as $N = 10^4$ molecules per cavity mode under the vibrational strong coupling condition. Future experimental and theoretical work is necessary to address this fundamental question.

Figure 5c,d further explores the effects of having disorders in C_i , using the exact expression for $J_{\text{eff}}(\omega)$. Figure 5c shows the cavity frequency dependence of k/k_0 for $N = 10^3$ at a collective Rabi splitting of $\Omega_{\rm R}$ = 100 cm⁻¹. The values of C_i are taken from a normal distribution with standard deviation σ_Q , while Λ is kept constant, and there is no angle disorder for the lightmatter couplings, such that $\chi = 1$ (cf. eq 9). As shown in Figure 5c, increasing the disorder in the coupling (increasing σ_{Q}) decreases the cavity effects. This is because adding disorder to the couplings allows the dark states coupling to R_0 to show up in $J_{\text{eff}}(\omega)$ (see Supporting Information 5, Figure S9), thus reducing the cavity effect as these dark modes have the same frequency as the vibrations outside the cavity. Nevertheless, the cavity modification effect will survive with a moderate magnitude of disorder, and the fundamental scaling indicated in eq 11 is also preserved (see Figure S9b in Supporting Information 5). We have also explored the inhomogeneous broadening of the solvent frequency $\omega_{\rm O}$ using Gaussian static disorders, with details provided in Supporting Information 5, Figure S10. We found that increasing the magnitude of the static disorder slightly decreases the value of k/k_0 , but it does not change the sharp resonance behavior of its cavity frequency dependence.

Figure 5d shows k/k_0 for N = 1000 at resonance and $\Omega_{\rm R} = 100 \text{ cm}^{-1}$, with C_j disorder sampled from a normal distribution with standard deviation σ_Q and the random distribution of the angle between the dipole and cavity field $\{\varphi_j\} \in [0, \varphi]$, with φ changing from 0 (fully ordered) to π (isotropic). One can see that with a small C_i disorder, the collective VSC effect will

survive even for a random disorder of dipole angle for $\{\varphi_j\} \in [0, 3\pi/4]$, as dark modes have a small contribution in the spectral density (see Figure S9 of Supplementary Note 5). Here, we demonstrate that the extent of the dark states highly depends on the disorder of the system, where the cavity can modify the reaction rates even in the presence of such states.

Resonance at the Normal Incidence. The dispersion relation of a FP microcavity^{12,17,64} is

$$\omega_{\mathbf{k}}(k_{\parallel}) = \frac{c}{n_{\rm c}} \sqrt{k_{\perp}^2 + k_{\parallel}^2} \tag{12}$$

where *c* is the speed of light in vacuum, and we have assumed the refractive index inside the cavity $n_c \approx 1$. The expression of the many-mode Hamiltonian is provided in Supporting Information 9, Section A. When $k_{\parallel} = 0$ (or $\theta = 0$), the photon frequency is $\omega_c \equiv \omega_k(k_{\parallel} = 0) = ck_{\perp}$, which is the cavity frequency we introduced in eq 4. Experimentally, it is observed that only at $k_{\parallel} = 0$, $\omega_k = \omega_Q$ (known as the normal incidence condition) will there be VSC effects.^{2,7,65} Here, we generalize the single-mode expression in eq 10 into many modes to understand the normal incidence condition. By considering many modes, the FGR rate constant inside a 1D FP cavity (1dimension along the k_{\parallel} direction) reduces back to the single mode case because of the van-Hove-type singularity⁶⁶ in the photonic DOS.⁴⁶ As a result, inside a 1D FP cavity, VSC modification occurs only at the normal incidence $\omega_c = \omega_0$.

For molecules coupled inside a 2D FP cavity (2-dimensional along the in-plane direction), the FGR rate constant is expressed as follows

 $k_{\rm VSC}^{\rm 2D}$

$$= 2 \left| \Delta_{x} \right|^{2} \int_{0}^{\infty} d\omega \frac{\Lambda \omega_{\mathbf{Q}}^{2} \cdot \omega \Gamma_{\mathbf{Q}}^{2\mathrm{D}}(\omega) \cdot \mathcal{A}_{0}(\omega - \omega_{0}) \cdot e^{-\beta \hbar \omega_{0}}}{\left[\omega_{\mathbf{Q}}^{2} - \omega^{2} + \tilde{\mathcal{R}}^{2\mathrm{D}}(\omega) \right]^{2} + \left[\omega \Gamma_{\mathbf{Q}}^{2\mathrm{D}}(\omega) \right]^{2}},$$
(13)

where $\Gamma_{\rm O}^{\rm 2D}(\omega)$ and $\tilde{\mathcal{R}}^{\rm 2D}(\omega)$ are generalized expressions for a 2D FP cavity, both of which contain the effective photon lifetime due to propagation in the in-plane direction⁴⁶ $\tau_{\parallel}(\omega) = \mathcal{D}_{\sqrt{k_{\perp}^2 + k_{\parallel}^2/(c \cdot k_{\parallel})}}$ with \mathcal{D} as the effective mode diameter.⁴⁶ The detailed expressions are provided in Supporting Information 9. The effective photon lifetime has a maximum value at $k_{\parallel} = 0$, leading to the largest magnitude of rate constant suppression. The finite in-plane momentum of the mode effectively decreases the effective lifetime of the thermal photon in a given mode volume.⁴⁶ Note that the interpretation of $\tau_{\parallel}(\tilde{\omega})$ is consistent with the polariton transport picture, ^{52,67–69} because for $k_{\parallel} = 0$, the group velocity for photon and polariton is zero, leading to no transport. And for $k_{\parallel} > 0$, the group velocity for thermal photons is fast, leading it to travel a large distance and not be confined in a given region.⁴⁶ Overall, this leads to a sharp resonance at ω_c = $\omega_{\rm O}$ when $k_{\parallel} = 0$. The rate constant expression $k_{\rm VSC}^{\rm 2D}$ (eq 13) is the third key result of this paper, which predicts that the maximum suppression of k/k_0 happens at the normal incidence at $k_{\parallel} = 0$.

Figure 6 presents the VSC-suppressed rate constant using the FGR expression (eq 10) under different Rabi splitting $\Omega_{\rm R}$ values and a cavity lifetime $\tau_{\rm c}$ = 500 fs. Here, we consider the molecule coupled inside (a) a 1D FP cavity and (b) a 2D FP cavity. Figure 6a presents the results of k/k_0 value using eq 10 (dashed line) or numerically evaluating the frequency integral

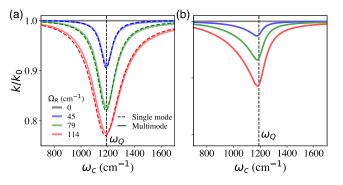


Figure 6. Normal Incidence effect for an 1D and 2D FP cavity. FGR rate profiles of k/k_0 as a function of ω_{c} where the cavity lifetime is τ_c = 500 fs. Results are presented for various light-matter coupling strengths. (a) FGR rate profiles inside a 1D FP cavity. (b) FGR rate profiles for many mode cases inside a 2D FP cavity.

related to the photonic DOS (solid line). The result is visually (near) identical to the single-mode case due to the van-Hovetype singularity in the 1D DOS, depicted in the dashed curve. Figure 6b presents k/k_0 for many Q_j DOF coupled to many modes inside a 2D FP cavity, using eq 7, and the $k_{\rm VSC}^{\rm 2D}$ expression in eq 13, with the effective mode diameter $\mathcal{D} = 3.33 \,\mu\text{m}$, which is a typical value estimated⁴⁶ from the VSC experiments.⁴⁸ One can see that the resonance peak is still sharply centered around $\omega_c = \omega_{Q_2}$ where ω_c is the normal incidence frequency in a 2D FP cavity. The theory, $k_{\rm VSC}^{\rm 2D}$ in eq 13 thus exhibits the features of (1) resonance condition, (2) normal incidence condition and operates under the (3) collective coupling regime and (4) thermally activated condition.

CONCLUSIONS

To summarize, we present a microscopic mechanism and an analytic rate theory that provide theoretical insights into the resonance VSC suppression of the rate constant under normalincidence conditions, collective light-matter coupling, and the thermally activated regime. For the model reaction, the reactant vibrational excitation $|\nu_{\rm L}\rangle \rightarrow |\nu'_{\rm L}\rangle$ is the rate-limiting step and thus controls the overall apparent rate constant. Coupling to the cavity explicitly splits the effective solvent spectral density that influences the dynamics of the reaction coordinate (see Figure 2a), and thus reduces the thermal activation rate k_1 , hence reducing the overall apparent rate constant. For a single molecule coupled to a single mode cavity, the theory $k_{\rm VSC}$ (eq 10) exhibits (i) a sharp resonance suppression behavior^{1,7} at $\omega_{\rm c} = \omega_{\rm Q}$ (Figure 2); (ii) nonlinear scaling^{1,4} of k/k_0 with respect to $\Omega_{\rm R}$ (Figure 3a), as well as the nonlinear scaling^{1,4} of $\Delta\Delta G^{\ddagger}$ with respect to Ω_{R} ; (iii) modification of both effective activation Entropy and Enthalpy⁴ (Figure 3b). (iv) The null effect^{60,61} because of a very low reaction barrier (Figure 4), such that the mechanistic in eq 6 no longer hold. The analytic theory (eq 7) agrees very well with the numerically exact simulations for all cases. The theory $k_{\rm VSC}$ (eq 10) also exhibits the collective effect, where both the collective solvent-solute coupling Λ as well as the collective light-matter coupling Ω_R show up in the rate constant expression. The theory k_{VSC}^{2D} in eq 13 thus demonstrates all key features in the VSC experiments.

The theory (eq 10 or eq 13) has several interesting predictions that can be experimentally tested. (a) The magnitude of the VSC effect on rate constant scales (eq 11) as $\Omega_{\rm R}^2$ or N, which should be experimentally checked. (b) For two chemically similar reactions, if one operates under the mechanism in eq 6 and satisfies $k_1 \ll k_2$, k_3 but the other does not (due to the low reaction barrier), then the current theory predicts that there will be a VSC effect for the first reaction but not for the second one. (c) Based on $k_{\text{VSC}}^{\text{2D}}$ (eq 13), the action spectrum should have a longer tail at the red frequency (ω_c < $\omega_{\rm O}$). Based on the current theory, we recommend future experimental investigations to focus on (1) confirming the scaling relation of k/k_0 with respect to Ω_R (or N) with more data points. (2) confirming potentially null VSC results in the alcoholysis reaction between 2,4-toluene-diisocyanate and chloralhydrate due to its low barrier,⁶² which will greatly inform the VSC mechanism, given that the similar alcoholysis reaction between phenylisocyanate and cyclohexanol has shown VSC resonance suppression effects.⁷ (3) More data points on the cavity frequency dependence of k/k_0 to provide the shape of the action spectrum. (4) control the dipole orientations^{70,71} (so one can control χ in eq 9) and measure the corresponding VSC effects.

The cavity-mediated vibrational energy transfer process has been experimentally verified when the system is directly pumped into polariton states (as opposed to the VSC ground state reactions, which occur under dark and thermally activated conditions). These experiments by Xiong and co-workers,⁷² together with the cavity Molecular Dynamics simulations^{29,73,74} and the FGR type of theory,^{30,39} indicate that the cavity can indeed mediate the vibrational energy transfer rates under the nonequilibrium polariton pumping conditions. These experiments⁷² and theoretical works may be closely connected with the currently investigated VSC reactions. Using simple models to understand those nonequilibrium pumping VSC experiments⁷² would also be valuable, as this could indirectly probe the fundamental mechanism of the VSC-modified rate constant. We also need to point out the limitations of the model systems in eq 2. Although it could be an appropriate model for describing the vibrational energy transfer between solute and solvent,²⁹ any potentially relevant anharmonic interaction effects are not captured by the bilinear interaction term in eq 2 of the present manuscript.

The current rate theory (eqs 10 or eq 13) requires several key parameters as input, including the collective light-matter coupling $\Omega_{\rm R}$, Q mode reorganization energy Λ , cavity frequency ω_{σ} etc. These key parameters can be extracted from ab initio simulations of a particular reaction²⁸ or atomistic cavity molecular dynamics simulations,²⁹ as well as from experiments that often report line shape. In an analogy, the situation is similar to Marcus theory in electron transfer reactions, where key parameters are required before one can use it as a predictive rate constant expression.

ASSOCIATED CONTENT

③ Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/jacs.5c03182.

Details of model systems; exact quantum dynamics using hierarchical equations of motion; rate constant calculations; derivation of $J_{\text{eff}}(\omega)$; $J_{\text{eff}}(\omega)$ simplification and scaling analysis; normal mode analysis; cavity lifetime dependence; many modes Hamiltonian and the normal incidence condition for VSC effects (PDF)

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Notes

The authors declare no competing financial interest.

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